Real-World Learning with Markov Logic Networks

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(Joint work with Parag & Matt Richardson)

Overview

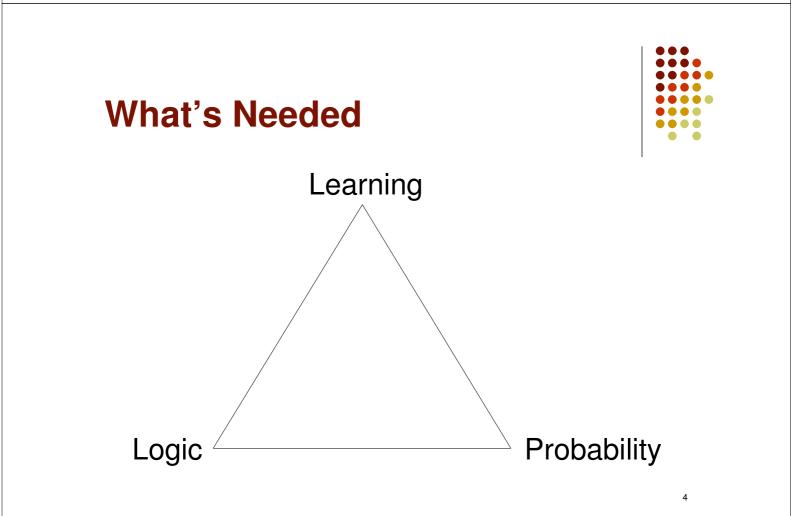
- Motivation
- Background
- Markov logic networks
- Inference in MLNs
- Learning MLNs
- Experiments
- Discussion



Motivation



- Machine learning / data mining systems must work with less help from people
- Automate data cleaning and integration
- Handle multiple types of objects and relations
- Easily incorporate domain knowledge



State of the Art



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- Learning: Decision trees, SVMs, etc.
- Logic: Resolution, WalkSat, Prolog, description logics, etc.
- Probability: Bayes nets, Markov nets, etc.
- Learning + Logic: Inductive logic prog. (ILP)
- Learning + Probability: EM, K2, etc.
- Logic + Probability: Halpern, Bacchus, KBMC, PRISM, etc.

Learning + Logic + Probability

- Recent (last five years)
- Workshops: SRL ['00, '03, '04], MRDM ['02, '03, '04]
- Special issues: SIGKDD, Machine Learning
- All approaches so far use only subsets of first-order logic
 - Horn clauses (e.g., SLPs [Cussens, 2001; Muggleton, 2002])
 - Description logics (e.g., PRMs [Friedman et al., 1999])
 - Database queries (e.g., RMNs [Taskar et al., 2002])

Questions



- Is it possible to combine the full power of first-order logic and probabilistic graphical models in a single representation?
- Is it possible to reason and learn efficiently in such a representation?

Markov Logic Networks

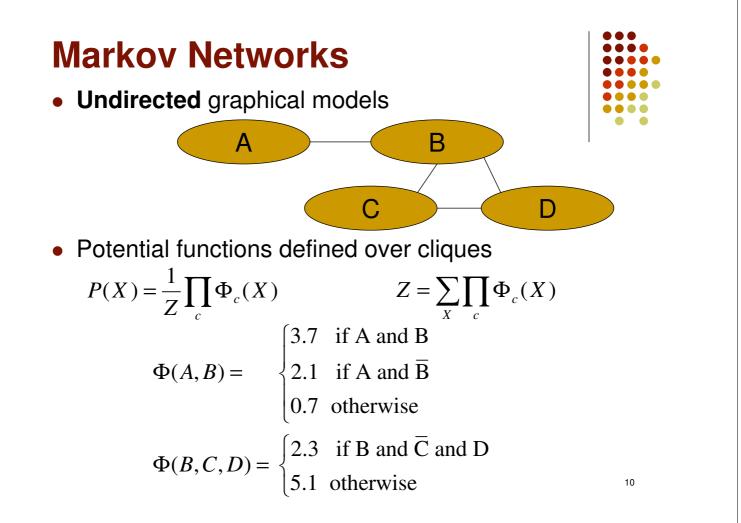
- **Syntax:** First-order logic + Weights
- Semantics: Templates for Markov nets
- Inference: KBMC + MCMC
- Learning: ILP + Pseudo-likelihood
- **Special cases:** Collective classification, link prediction, link-based clustering, social networks, object identification, etc.

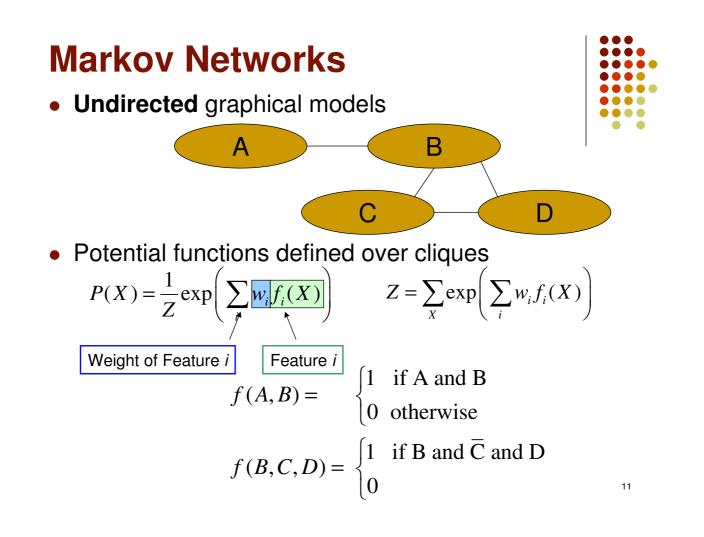


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First-Order Logic



- Constants, variables, functions, predicates
 E.g.: Anna, X, mother_of(X), friends(X, Y)
- Grounding: Replace all variables by constants E.g.: friends (Anna, Bob)
- World (model, interpretation): Assignment of truth values to all ground predicates



Smoking causes cancer Friends either both smoke or both don't smoke



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Example of First-Order KB

 $\forall x \ Smokes(x) \Rightarrow Cancer(x)$

 $\forall x, y \ Friends(x, y) \Rightarrow (Smokes(x) \Leftrightarrow Smokes(y))$

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Markov Logic Networks

- A logical KB is a set of hard constraints on the set of possible worlds
- Let's make them soft constraints: When a world violates a formula, It becomes less probable, not impossible
- Give each formula a weight (Higher weight ⇒ Stronger constraint)

 $P(world) \propto \exp(\sum weights of formulas it satisfies)$

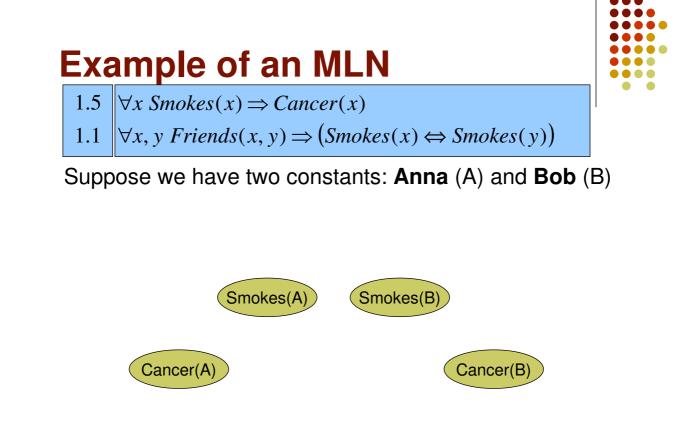


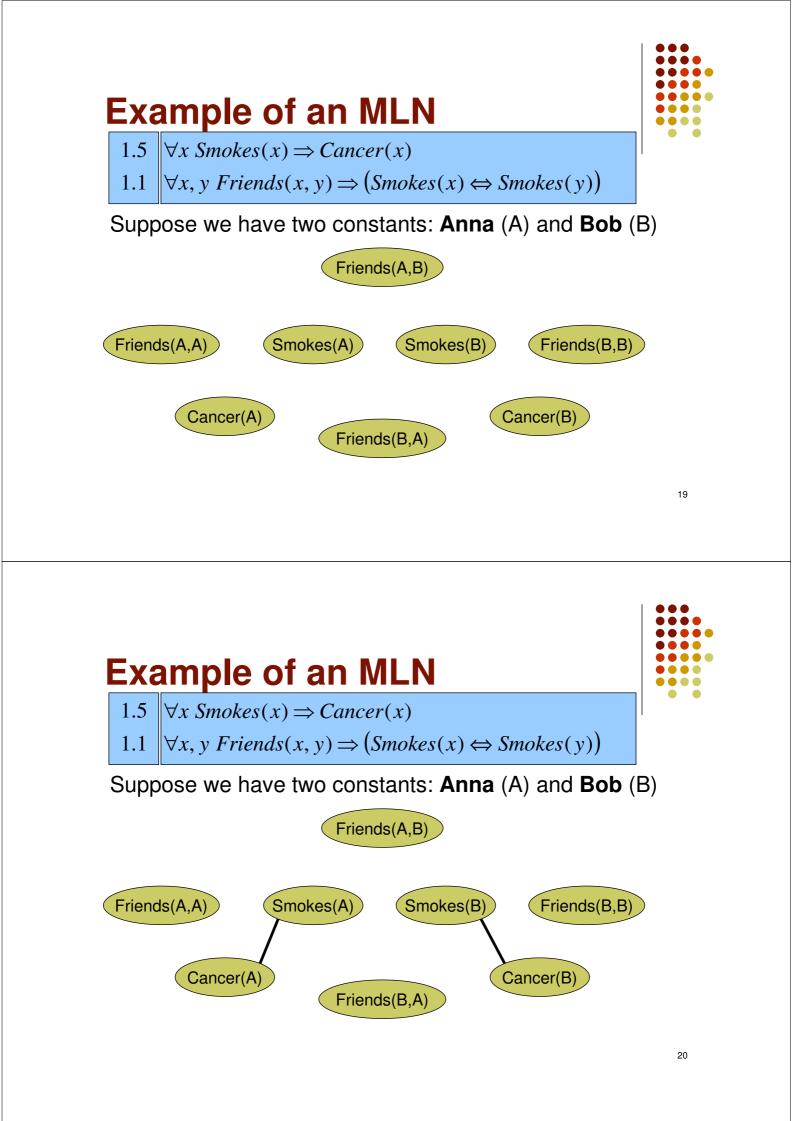


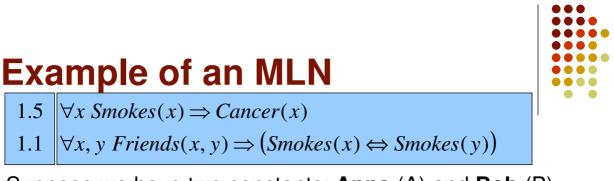
Definition



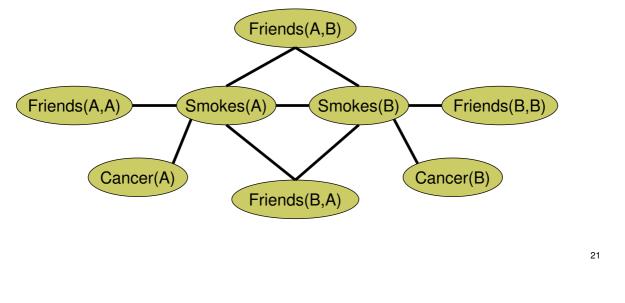
- A Markov Logic Network (MLN) is a set of pairs (F, w) where
 - F is a formula in first-order logic
 - w is a real number
- Together with a finite set of constants, it defines a Markov network with
 - One node for each grounding of each predicate in the MLN
 - One feature for each grounding of each formula F in the MLN, with the corresponding weight w







Suppose we have two constants: Anna (A) and Bob (B)



More on MLNs



- Graph structure: Arc between two nodes iff predicates appear together in some formula
- MLN is template for ground Markov nets
- Typed variables and constants greatly reduce size of ground Markov net
- Functions, existential quantifiers, etc.
- MLN without variables = Markov network (subsumes graphical models)

MLNs Subsume FOL



- Infinite weights \Rightarrow First-order logic
- Satisfiable KB, positive weights ⇒
 Satisfying assignments = Modes of distribution
- MLNs allow contradictions between formulas
- How to break KB into formulas?
 - Adding probability increases degrees of freedom
 - Knowledge engineering decision
 - Default: Convert to clausal form

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Inference



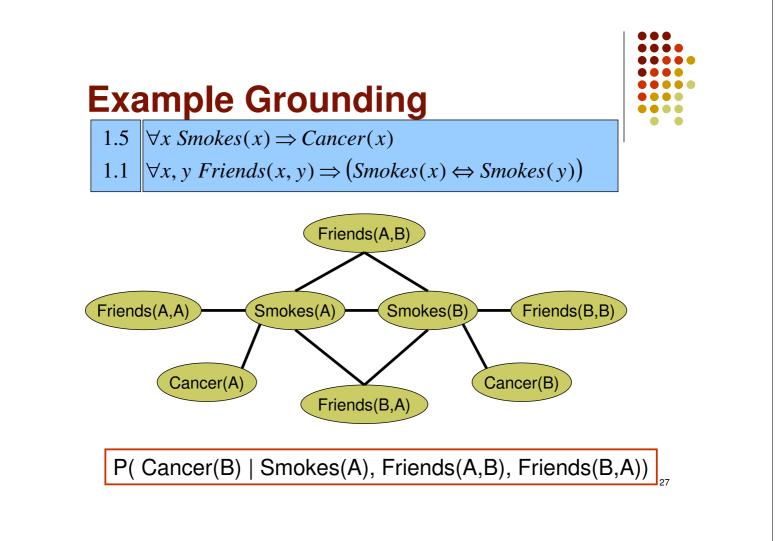
- Given query predicate(s) and evidence
 - 1. Extract minimal subset of ground Markov network required to answer query
 - 2. Apply probabilistic inference to this network

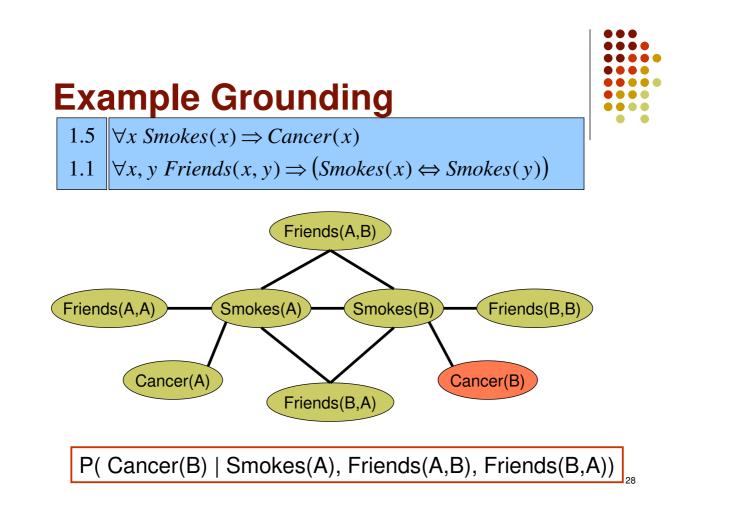
(Generalization of KBMC [Wellman et al., 1992])

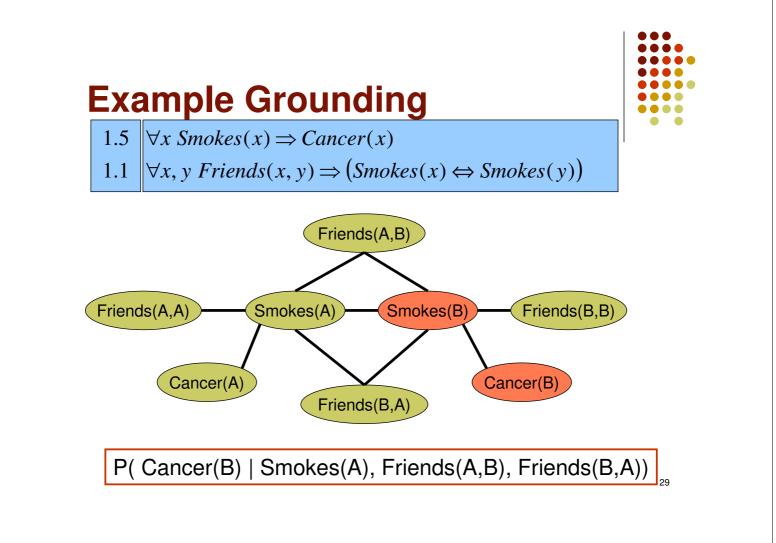
Grounding the Template

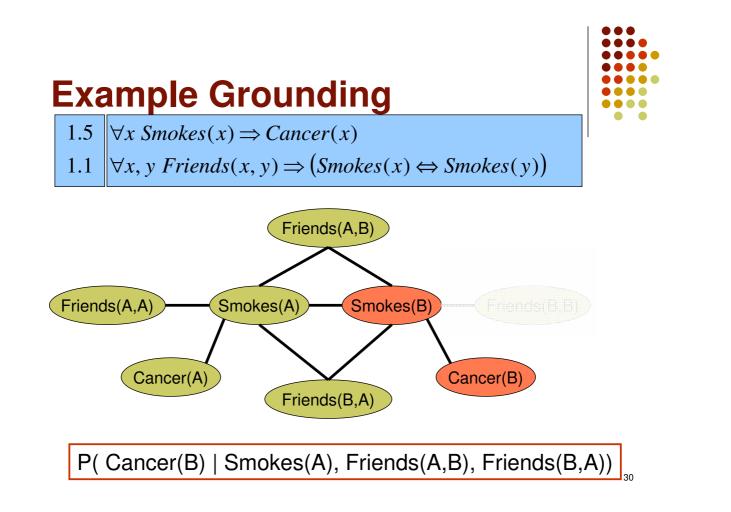


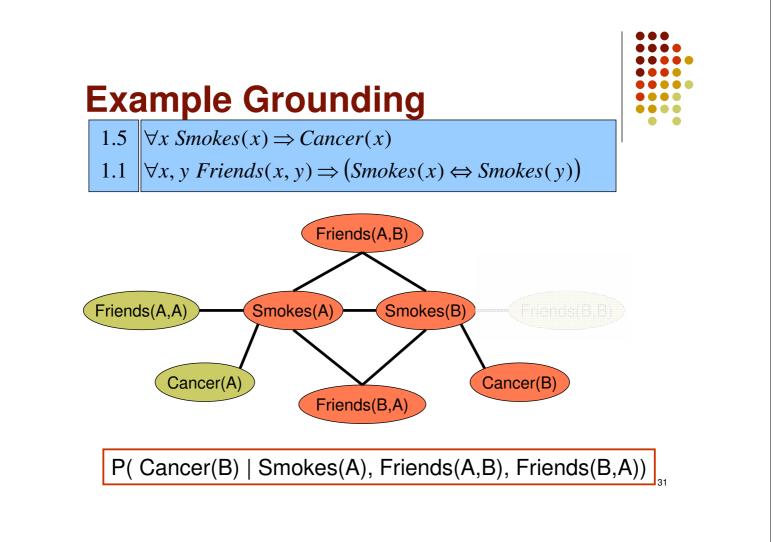
- Initialize Markov net to contain all query preds
- For each node in network
 - Add node's Markov blanket to network
 - Remove any evidence nodes
- Repeat until done

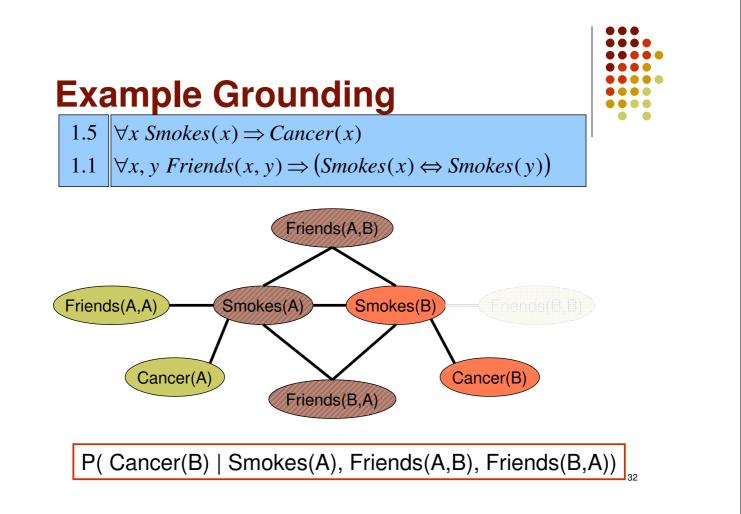


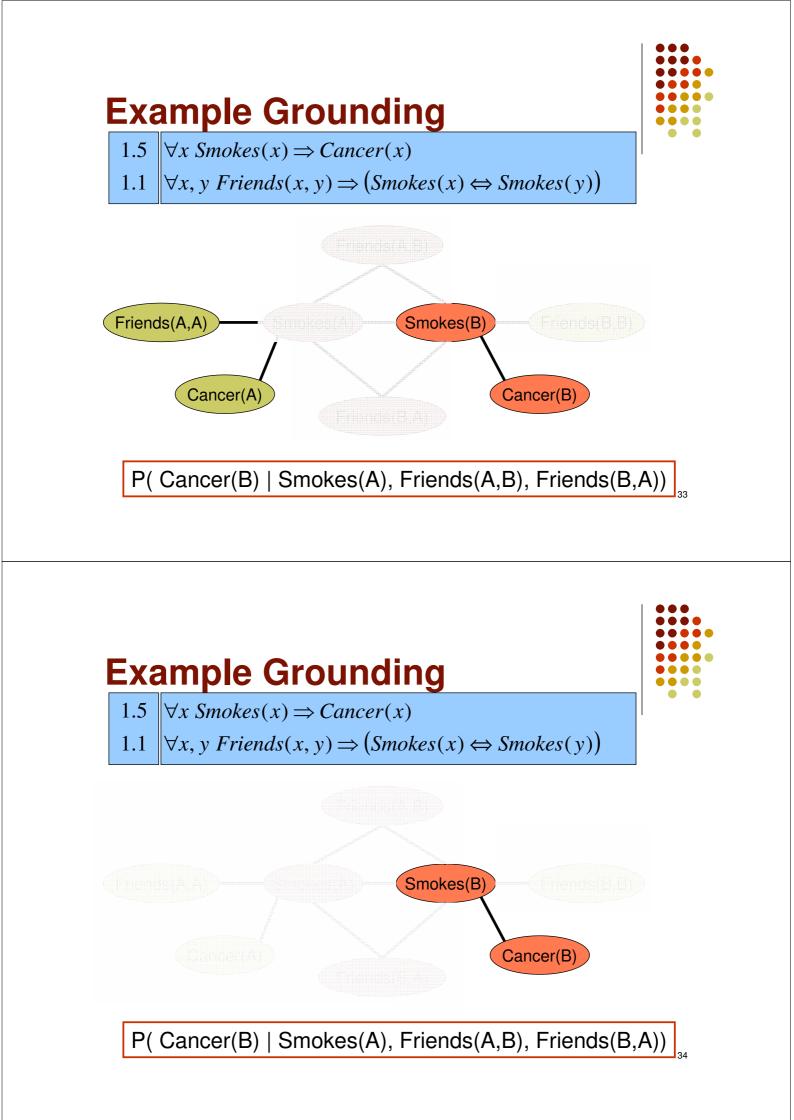


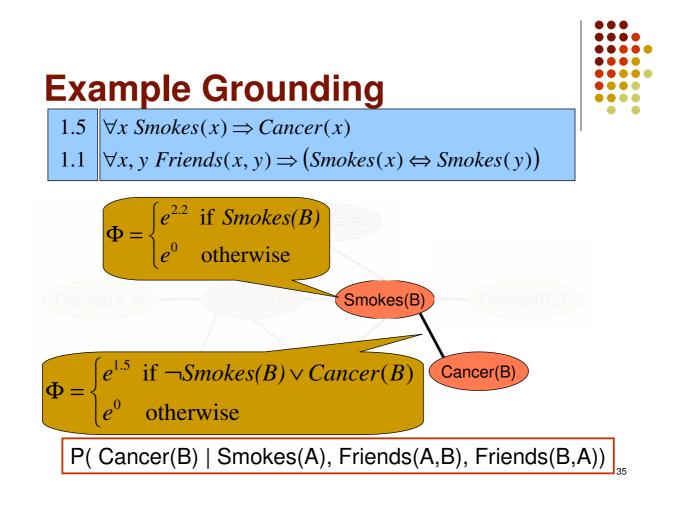












Probabilistic Inference



Recall

$$P(X) = \frac{1}{Z} \exp\left(\sum_{i} w_i f_i(X)\right) \qquad Z = \sum_{X} \exp\left(\sum_{i} w_i f_i(X)\right)$$

- Exact inference is #P-complete
- Conditioning on Markov blanket is easy:

$$P(x \mid MB(x)) = \frac{\exp\left(\sum_{i} w_{i} f_{i}(x)\right)}{\exp\left(\sum_{i} w_{i} f_{i}(x=0)\right) + \exp\left(\sum_{i} w_{i} f_{i}(x=1)\right)}$$

Gibbs sampling exploits this

Markov Chain Monte Carlo



Gibbs Sampler

- 1. Start with an initial assignment to nodes
- 2. One node at a time, sample node given others
- 3. Repeat
- 4. Use samples to compute P(X)
- Apply to ground network
- Many modes \Rightarrow Multiple chains
- Initialization: MaxWalkSat [Selman et al., 1996]

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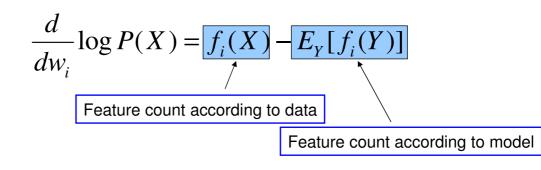


Learning

- Data is a relational database
- Closed world assumption
- Learning structure
 - Corresponds to feature induction in Markov nets
 - Learn / modify clauses
 - Inductive logic programming (e.g., CLAUDIEN [De Raedt & Dehaspe, 1997])
- Learning parameters (weights)

Learning Weights

- Maximize likelihood (or posterior)
- Use gradient ascent



Requires inference at each step (slow!)



Pseudo-Likelihood [Besag, 1975]

$$PL(X) \equiv \prod_{x} P(x \mid MB(x))$$

- Likelihood of each variable given its Markov blanket in the data
- Does not require inference at each step
- Very fast gradient ascent
- Widely used in spatial statistics, social networks, natural language processing

MLN Weight Learning



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- Parameter tying over groundings of same clause
- Maximize pseudo-likelihood using conjugate gradient with line minimization

$$\nabla_i = \sum_x nsat_i(x) - [p(x=0)nsat_i(x=0) + p(x=1)nsat_i(x=1)]$$

where $nsat_i(x=v)$ is the number of satisfied groundings of clause i **in the training data** when x takes value v

- Most terms not affected by changes in weights
- After initial setup, each iteration takes
 O(# ground predicates x # first-order clauses) 42

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Domain

- University of Washington CSE Dept.
- 24 first-order predicates: Professor, Student, TaughtBy, AuthorOf, AdvisedBy, etc.
- 2707 constants divided into 11 types: Person (400), Course (157), Paper (76), Quarter (14), etc.
- 8.2 million ground predicates
- 9834 ground predicates (tuples in database)

Systems Compared



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- Hand-built knowledge base (KB)
- ILP: CLAUDIEN [De Raedt & Dehaspe, 1997]
- Markov logic networks (MLNs)
 - Using KB
 - Using CLAUDIEN
 - Using KB + CLAUDIEN
- Bayesian network learner [Heckerman et al., 1995]
- Naïve Bayes [Domingos & Pazzani, 1997]

Sample Clauses in KB

- Students are not professors
- Each student has only one advisor
- If a student is an author of a paper, so is her advisor
- Advanced students only TA courses taught by their advisors
- At most one author of a given paper is a professor

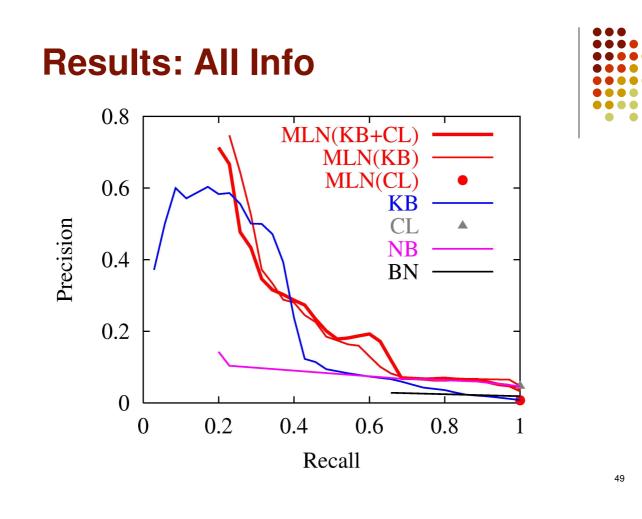
Methodology

- Data split into five areas: AI, graphics, languages, systems, theory
- Leave-one-area-out testing
- Task: Predict AdvisedBy(x, y)
 - All Info: Given all other predicates
 - Partial Info: With Student(x) and Professor(x) missing
- Evaluation measures:
 - Conditional log-likelihood (KB, CLAUDIEN: Run WalkSat 100x to get probabilities)
 - Area under precision-recall curve

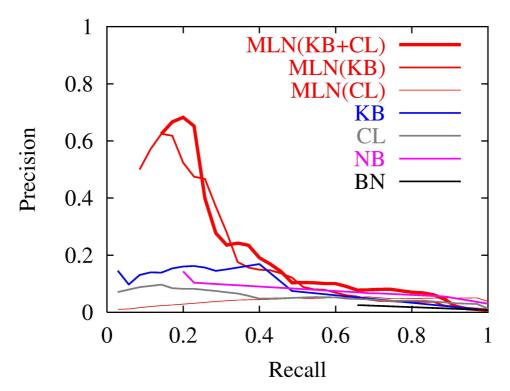
Results

System	All Info		Partial Info	
	CLL	Area	CLL	Area
MLN(KB+CL)	-0.044	0.27	-0.040	0.25
MLN(KB)	-0.047	0.25	-0.043	0.20
MLN(CL)	-0.341	0.02	-0.852	0.03
КВ	-0.124	0.16	-0.067	0.08
CL	-0.255	0.03	-0.371	0.04
NB	-0.218	0.17	-0.059	0.19
BN	-0.095	0.02	-0.166	0.04





Results: Partial Info





Efficiency



- Learning time: 88 mins
- Time to infer all 4900 AdvisedBy predicates:
 - With complete info: 23 mins
 - With partial info: 24 mins

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Related Work



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- Knowledge-based model construction [Wellman et al., 1992; etc.]
- Stochastic logic programs [Muggleton, 1996; Cussens, 1999; etc.]
- Probabilistic relational models [Friedman et al., 1999; etc.]
- Relational Markov networks [Taskar et al., 2002]
- Etc.

Special Cases of Markov Logic

- Collective classification
- Link prediction
- Link-based clustering
- Social network models
- Object identification
- Etc.

Future Work: Inference



- Lifted inference
- Better MCMC (e.g., Swendsen-Wang)
- Belief propagation
- Selective grounding
- Abstraction, summarization, multi-scale
- Special cases

Future Work: Learning

- Faster optimization
- Beyond pseudo-likelihood
- Discriminative training
- Learning and refining structure
- Learning by reformulation



- Object identification
- Information extraction & integration
- Semantic Web
- Social networks
- Assisted cognition
- Using world knowledge in parsing
- Using world knowledge in scene analysis
- Etc.

Conclusion

- Machine learning / data mining systems must work with less help from people
- Markov logic networks combine first-order logic and prob. graphical models
 - Syntax: First-order logic + Weights
 - Semantics: Templates for Markov networks
- Inference: MCMC over minimal grounding
- Learning: Pseudo-likelihood and ILP
- Experiments on UW DB show promise